

Economics 113 Professor Spearot
Introduction to Econometrics
Fall 2012 – Midterm 2
Name _____

ID _____

Midterm 2 – 70 Points

You must answer all questions. Please write your name on every page. The exam is closed book and closed notes. You may use calculators, but they must not be graphing calculators. Do not use your own scratch paper.

You must show your work to receive full credit

I have neither given nor received unauthorized aid on this examination, nor have I concealed any similar misconduct by others.

Signature _____

1. (45 Points) Suppose that you estimate sales by a firm as a function of the average education level of employees.

$$\log(\text{Sales}) = \beta_0 + \beta_{educ} \text{education} + u$$

Sales is measured in dollars per year, and *education* is measured in average years of post-secondary education across employees within the firm.

a.) Suppose you estimate $\hat{\beta}_{educ} = 0.07$. Please interpret this estimate. (5 Points)

b.) Supposing again that $\hat{\beta}_{educ} = 0.07$, and that the covariance between *education* and $\log(\text{Sales})$ is 2, what is the variance of *education* within the sample? (5 points)

- c.) Please state the four assumptions, and only four, that are required for unbiased estimates. (5 Points)
- d.) In running the regression, I forgot to include *technology*, which is a variable measuring the technology level of the firm's products. If *technology* is associated with higher sales, and higher technology products require a more educated workforce (i.e. they are positively correlated), in what direction, if any, is the estimate $\hat{\beta}_{educ}$ biased? Supposing that the original estimate of $\hat{\beta}_{educ}$ is positive, what can be said about the sign of β_{educ} ? (5 Points)
- e.) Suppose that I forgot to include the variable, *Holiday*, which is a dummy variable marking the Holiday period during which sales are usually *larger*. Suppose I say that the bias from forgetting about this variable is negative. What does this imply about the correlation between *education* and *Holiday*? Do you think this implies that we hire higher or lower quality workers during the holiday period? (5 Points)

f.) Please describe what it means for errors to be homoskedastic. (5 points)

g.) I report that the R^2 for the above regression is 0.10. What does this say about the model? What does this not say about the model? (5 points)

h.) Suppose that I double the size of the sample by replicating all observations once. What happens to the estimated variance of $\hat{\beta}_{educ}$ and why? (5 points)

i.) What is the most important thing you will learn in this class? (5 Points)

2. (25 Points) Using a sample of cars sold in California, I wish to estimate

$$MPG = \beta_0 + \beta_{GVW}GVW + u$$

MPG is miles per gallon of gas and GVW is gross vehicle weight measured in thousands of pounds.

- a.) Suppose you estimate that $\hat{\beta}_0 = 70$. Please interpret this estimate. Is this a sensible estimate to be interested in? (5 Points)
- b.) Suppose that $\hat{\beta}_{GVW} = -10$ using our first sample, but the true population value β_{GVW} is -15. Is this a problem? If our four assumptions for unbiasedness are satisfied, what must be the case for *future* estimates of $\hat{\beta}_{GVW}$ if we continually resample and estimate this relationship? (5 Points)
- c.) There are 0.45 kilograms per pound (approximately). If I measure GVW in kilograms, what does this do to the estimate $\hat{\beta}_{GVW} = -10$? (5 Points)

d.) Suppose instead that I estimate

$$\log(MPG) = \beta_0 + \beta_{GVW} \log(GVW) + u$$

Please **derive** using derivatives the interpretation for $\hat{\beta}_{GVW}$. Please state in words how we interpret $\hat{\beta}_{GVW}$.
(10 Points)

Please enjoy Halloween safely.